



# Safety Analysis for Reduction of Longitudinal Time Separation Minima on Oceanic Routes

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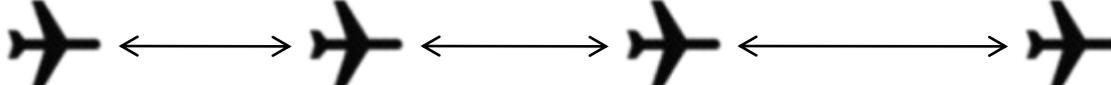
(Electronic Navigation Research Institute)

# Background (1)

- More efficient use of airspace is expected with the growth of air demand.
- Vertical separation
  - RVSM (Reduced Vertical Separation Minima)
    - Separation of the altitude is changed from 2000 ft to 1000 ft.
- Longitudinal separation
  - Distance based separation (50 NM/ 30NM)
    - An aircraft pair (ADS system and RNP/RNAV authorization required) can apply the distance based separation.

# Background (2)

- The time based separation (15 minutes) is still widely used.
  - There are still many aircraft without ADS system.
    - It costs more or less money to introduce and use ADS system.
- ➔ Reduced time based separation to 10 minutes is expected.

Minimum 15 min. 

Minimum 10 min. 

# Safety analysis

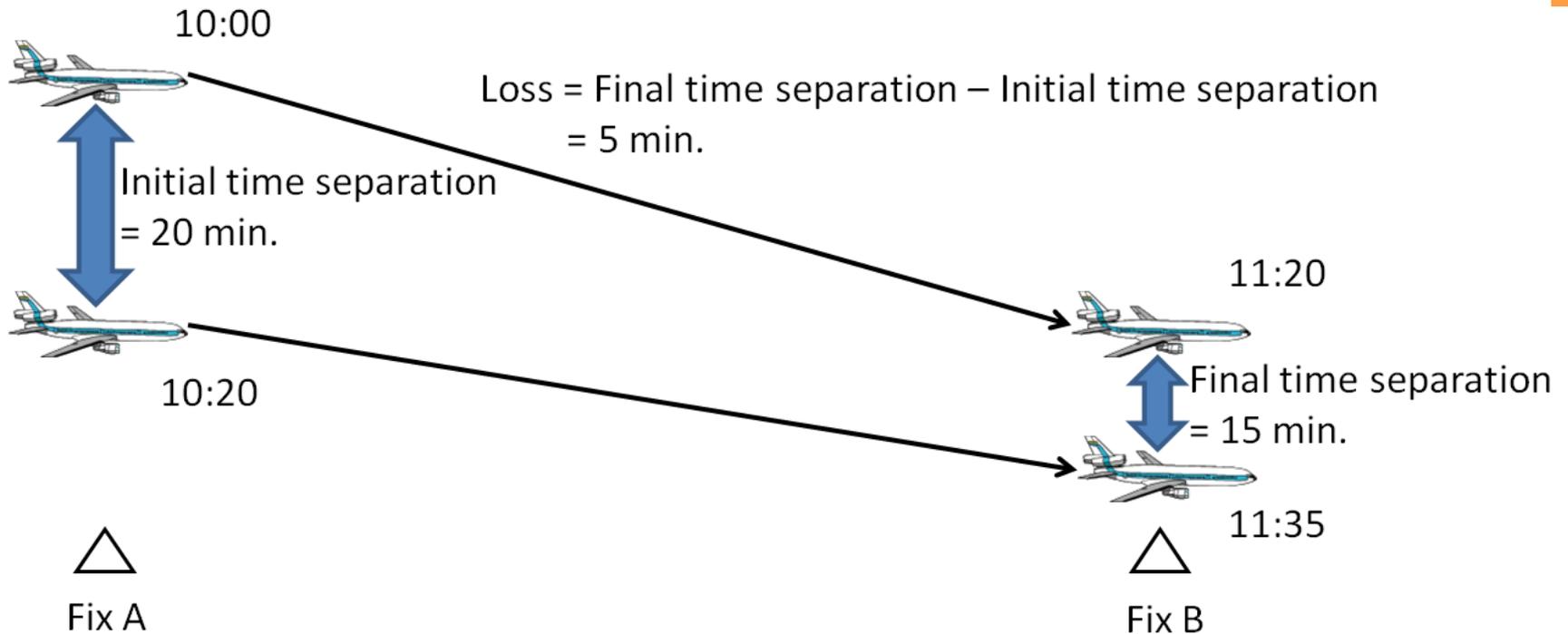
- When a new system is introduced, a safety analysis is required.
  - The target level of safety (TLS) in the en-route phase is set to  $5.0 \times 10^{-9}$  per flight hour in each dimension by ICAO.
  - Qualitative analysis is also required.
  - ➔ This time, the risk of collision between two aircraft is calculated based on the aircraft navigation performance.

# How to calculate the risk of collision

$$N_{ax} = P_y(0)P_z(0) \frac{2\lambda_x}{|\dot{x}|T} \left[ \frac{|\bar{\dot{x}}|}{2\lambda_x} + \frac{|\bar{\dot{y}}(0)|}{2\lambda_y} + \frac{|\bar{\dot{z}}(0)|}{2\lambda_z} \right] \sum E_x(t)Q_x(t)$$
$$= \underbrace{P_y(0)}_{\text{lateral}} \cdot \underbrace{P_z(0)}_{\text{vertical}} \cdot \underbrace{P_x(0)}_{\text{longitudinal}}$$

- A collision happens when a pair of aircraft is superposed vertically, laterally, and longitudinally.
  - $P_y(0) = 0.20$
  - $P_z(0) = 0.5380$
  - How to estimate  $P_x(0)$  ?

# Conventional loss distribution



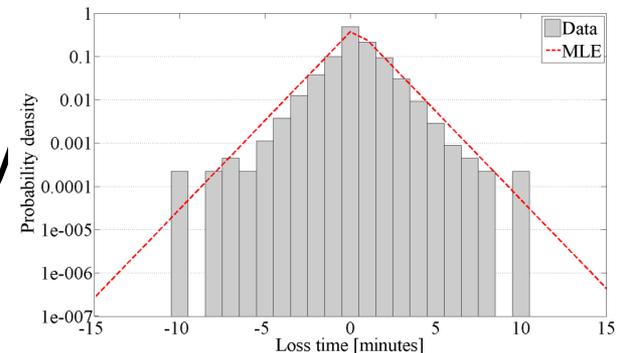
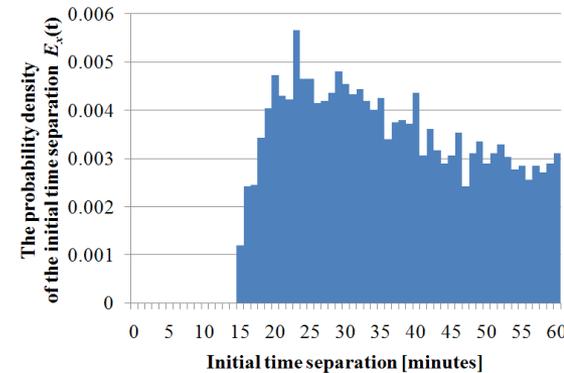
- Loss time > Initial time separation  
→ Infringed longitudinal separation.

# How to calculate $P_x(0)$

$$P_x(0) \propto \int E_x(t) Q_x(t) dt$$

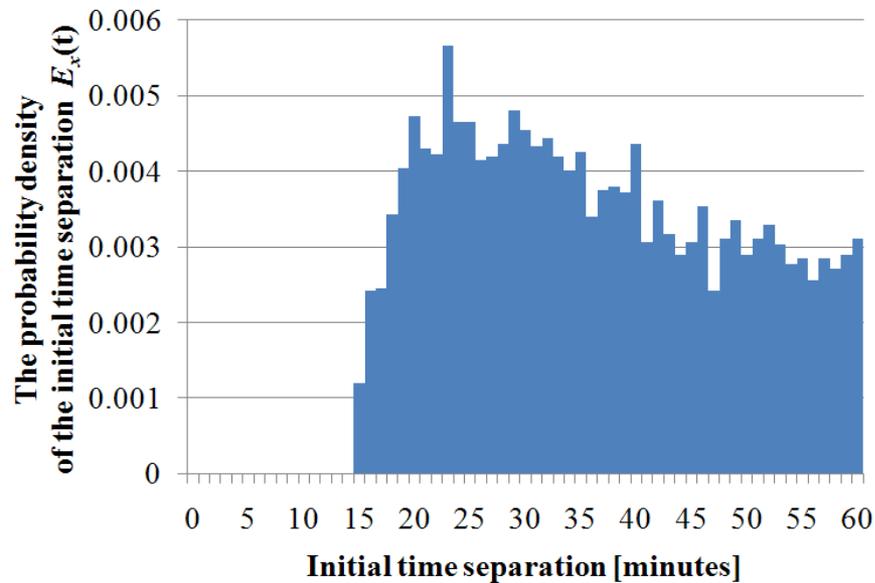
$$Q_x(t) = \int_t^{\infty} l(\tau) d\tau$$

- $E_x(t)$ : The proportion of the initial time separation equal to  $t$ .
- $Q_x(t)$ : The probability of the loss time greater than  $t$ .
- $L(t)$ : The probability density function of the loss time.

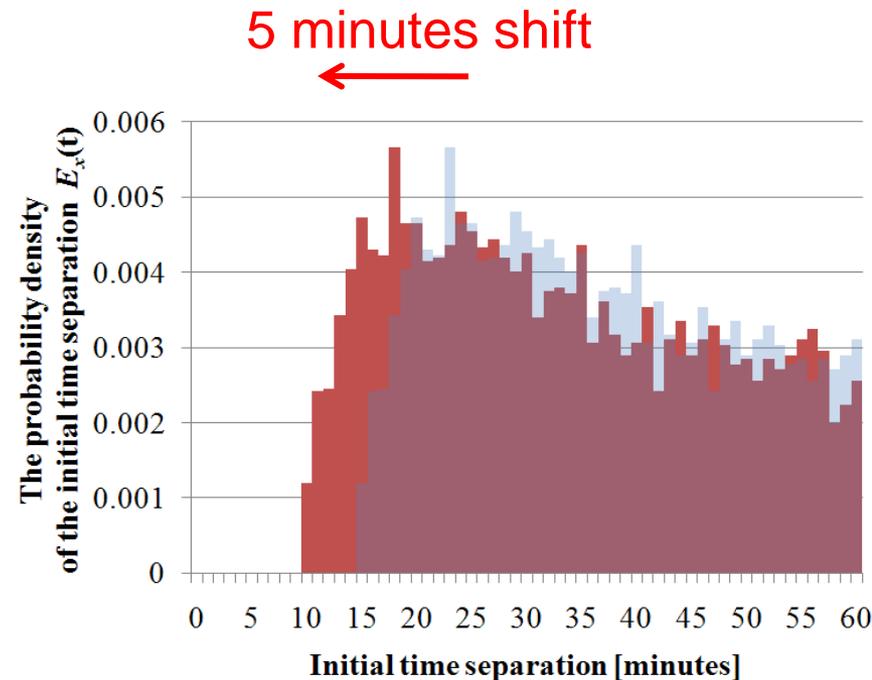




# Initial time separation (Ext)



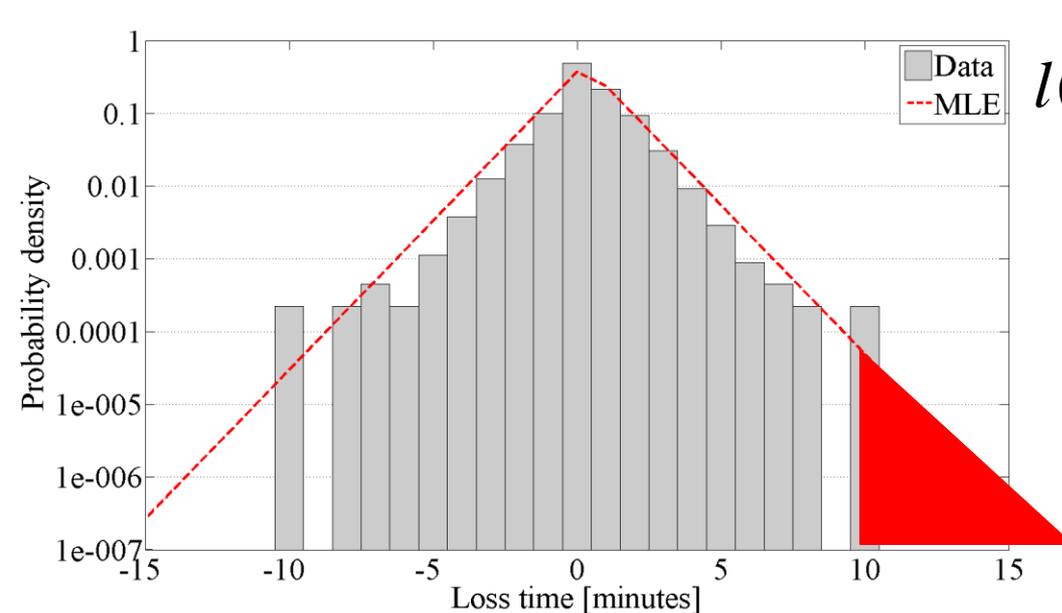
Obtained distribution in Airspace A  
(The minimum is 15 min.)



Estimated distribution in Airspace A  
(The minimum is 10 min.)

# Loss distribution (Lt)

- Loss distribution is modeled by double exponential (Laplace) distribution.
  - The loss distribution is obtained only when the Initial time separation is less than 60 minutes.
  - The loss time is discretized by 1 minute.



$$l(t; \mu, \lambda) = \frac{1}{2\lambda} \exp\left(\frac{-|t - \mu|}{\lambda}\right)$$

$$Q_x(t) = \int_t^{\infty} l(\tau) d\tau$$

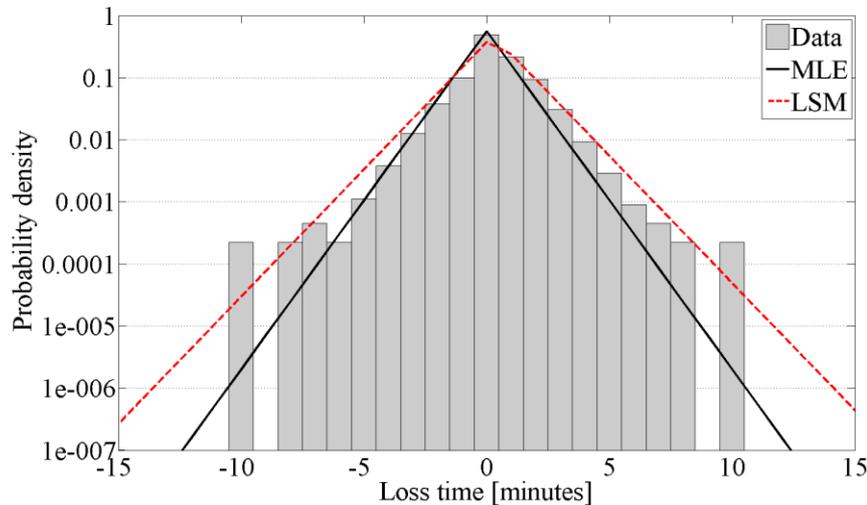
# Parameter estimation

- MLE (Maximum Likelihood Estimation)

$$lik = \prod_{i=1}^n \frac{1}{2\lambda} \exp\left(\frac{-|t_i - \mu|}{\lambda}\right) \text{ is maximized.}$$

- LSM (Least Square Method)

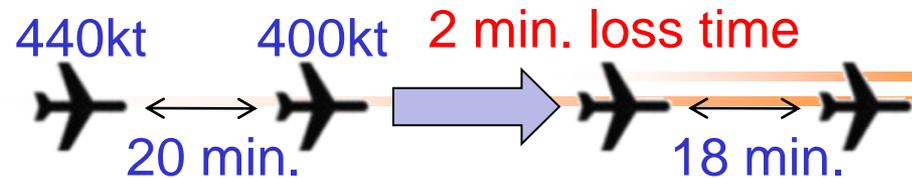
$$F = \sum_t [ \log(p_{act}(t)) - \log(p_{est}(t)) ]^2 \text{ is minimized.}$$



# The expected risk of collision

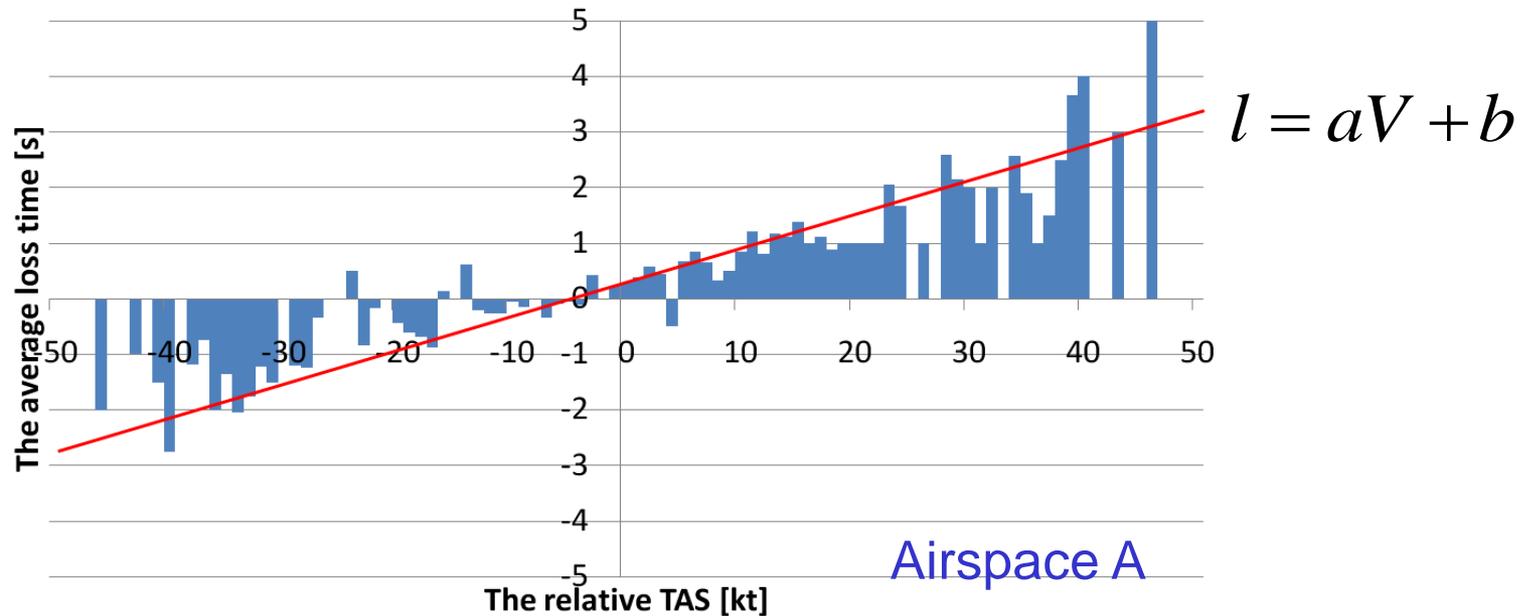
- The expected risk of collision is calculated assuming that the minimum initial time separation is set to 10 minutes.
  - Airspace A:  $4.977 \times 10^{-8}$
  - Airspace B:  $2.688 \times 10^{-8}$
  - TLS:  $5.0 \times 10^{-9}$
- The risk of collision is greater than the TLS. Is it risky to introduce 10 min. time separation?
  - ➔ The conventional calculation method causes an over-estimation.

# Reasons for over-estimation



- The relative speed
  - The distribution model is usually used to model the uncertainty of the system.
  - Assuming that the following aircraft flies faster than the preceding aircraft, a positive loss time is to be expected.
- The range of the initial time separation consisting of the loss distribution
  - Why does the loss distribution consist of the data which have less than **60 minutes** initial time separation?
  - The loss distribution by 60 minutes initial time separation and 15 minutes initial time separation can be different according to some factors (wind conditions..).

# The relationship between loss time & relative speed



- A positive relative TAS (true air speed) is defined in the case when the following aircraft flies faster than the preceding aircraft.
- There seems to be a relationship between the relative TAS & the average loss time.

# Refined loss time

- Refined loss time:  $t_i^{new} = t_i - (a\Delta V_i + b)$
- Refined loss distribution:  $l_m^{new}(t)$
- The probability that the loss time is greater than t:  $Q_x^{new}(t) = \sum_{\Delta V} e(\Delta V) \int_t^{\infty} l_m^{new}(\tau - (a\Delta V + b)) d\tau$

The relative TAS \* the refined loss time  
Original loss time distribution } can be different.

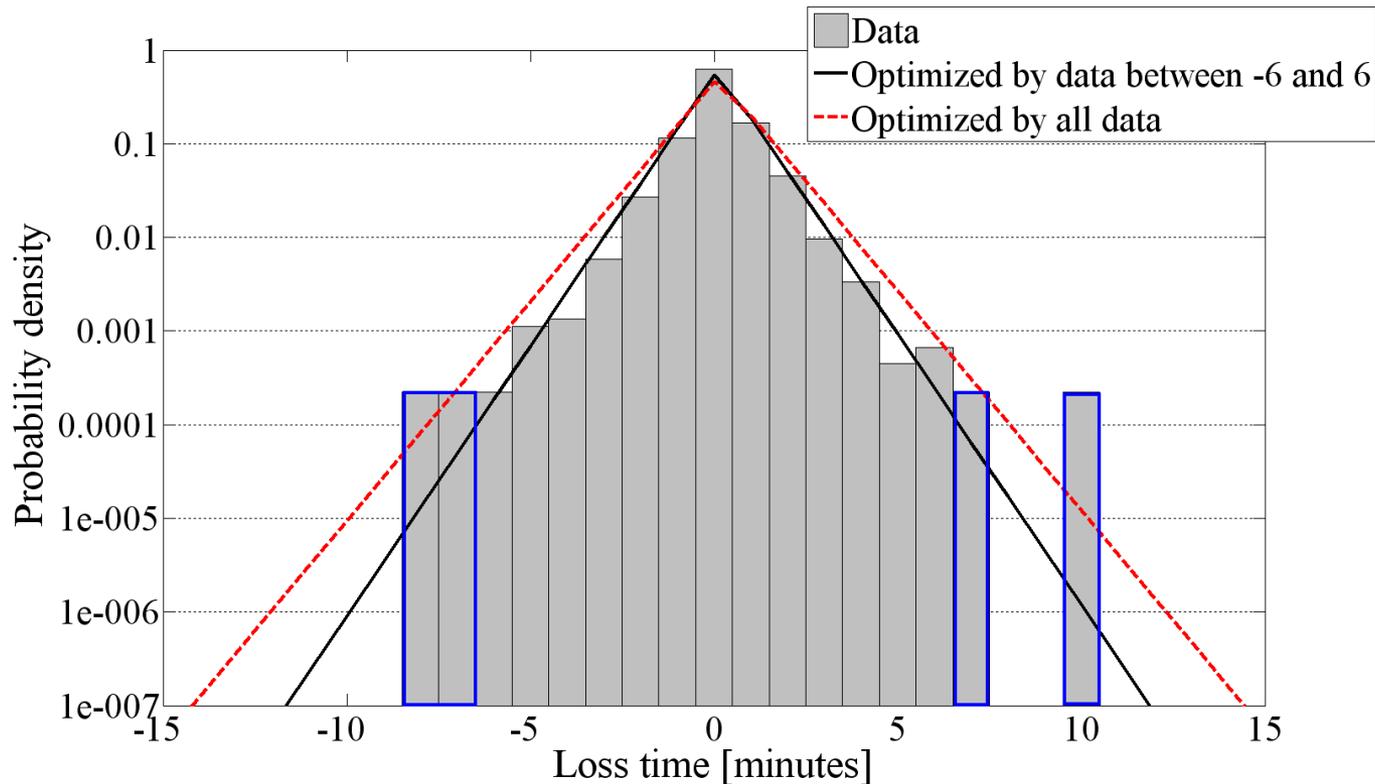
- The distribution of the convolution of the two dependent parameters can be different from the original distribution.

# Refined risk of collision (1)

	Risk of collision considering relative TAS	Risk of collision by conventional method
Airspace A	$1.949 \times 10^{-8}$	$4.977 \times 10^{-8}$
Airspace B	$5.462 \times 10^{-9}$	$2.688 \times 10^{-8}$
TLS	$5.0 \times 10^{-9}$	

- The risk of collision is decreased when the relative TAS is considered, but is still greater than the TLS.  
→ Next, the range of the initial time separation consisting of the loss distribution is considered.

# Abnormal values



- The black line fits better with the data between -6 and 6 minutes.
  - The distribution gets wider wrongly because of a few abnormal values surrounded by blue rectangles.

# Number of abnormal values

Initial time separation $x$	Airspace A	Airspace B
$0 < x \leq 20$	0/526	0/506
$20 < x \leq 30$	0/1358	0/1262
$30 < x \leq 40$	1/1187	4/1115
$40 < x \leq 50$	1/972	2/862
$50 < x \leq 60$	2/761	2/722

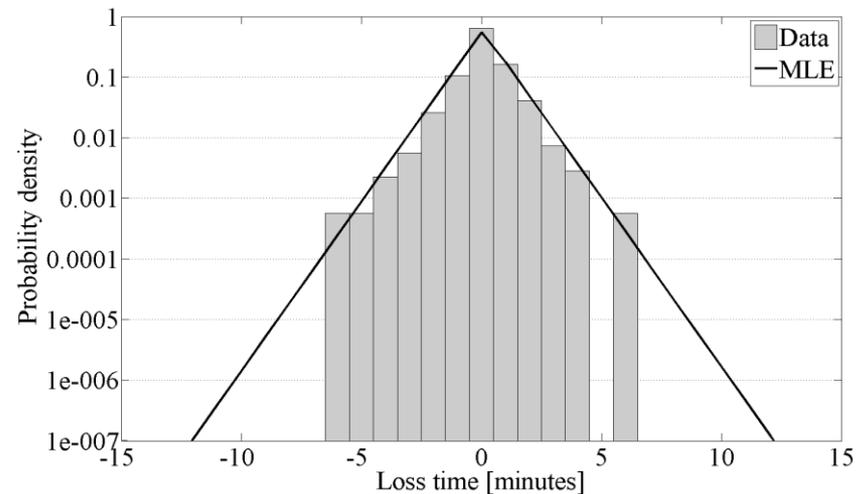
The number of abnormal values / The number of all data

- The result implies that the number of abnormal values depends on the initial time separation.
  - ➔ Check by binomial test
    - It CANNOT be said that the number of the abnormal values is NOT related to the initial time separation.

# The refined risk of collision (2)

	Risk of collision considering relative TAS & 30 min. initial time separation	Risk of collision considering relative TAS	Risk of collision by conventional method
Airspace A	$2.394 \times 10^{-9}$	$1.949 \times 10^{-8}$	$4.977 \times 10^{-8}$
Airspace B	$1.425 \times 10^{-10}$	$5.462 \times 10^{-9}$	$2.688 \times 10^{-8}$
TLS	$5.0 \times 10^{-9}$		

- The risk of collision is smaller than the TLS in each airspace.



# Conclusions

- A safety analysis was conducted under 10 minutes time-based separation in Fukuoka FIR.
  - The conventional safety assessment was likely to cause an over-estimation
    - ➔ Two factors were considered:
      - The relative true airspeed
      - The initial time separation
    - Using the refined method, it was proven that the risk of collision was less than the TLS.

This safety analysis was conducted under just one hazardous condition.