



# Study of INS–Aided GPS Tracking Performance under Simulated Ionospheric Scintillation Associated with Plasma Bubbles

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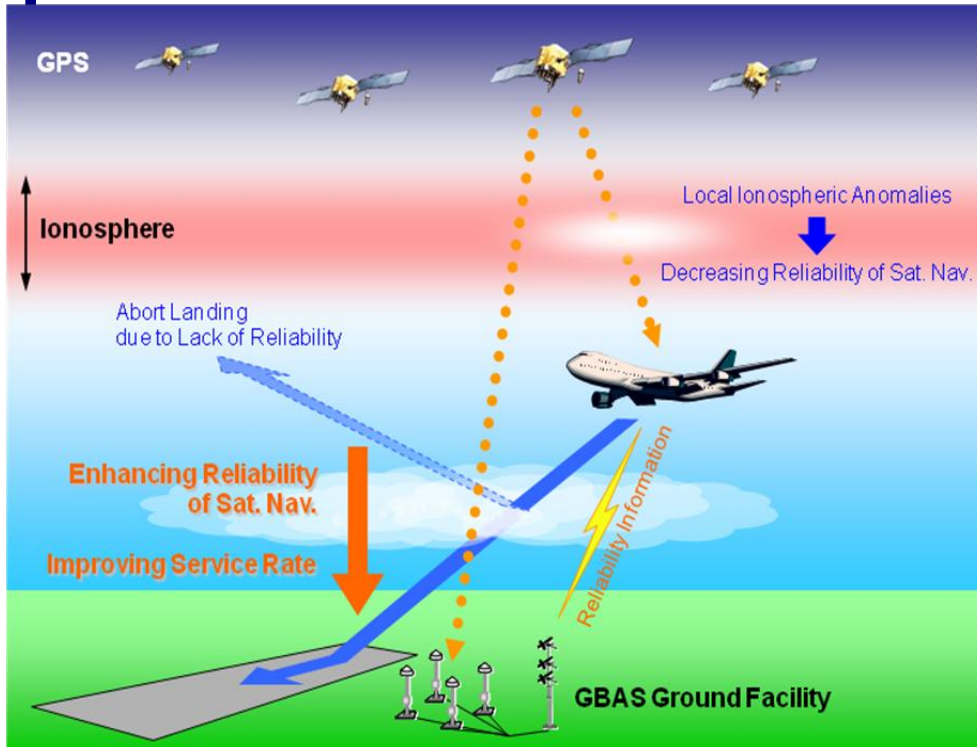
and

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Electronic Navigation Research Institute (ENRI)





# Background (1/2)



Ionospheric effects would degrade availability of aircraft precision approach

## GBAS

- ① Spatial gradient of TEC would result in wrong correction data
- ② Scintillation would cause temporal loss of satellite lock  
→ re-initialization of PR smoothing  
→ go around due to multiple satellites losses

## Purpose of this paper

Evaluation of INS-aiding under scintillation

← Robust Tracking by INS-Aiding

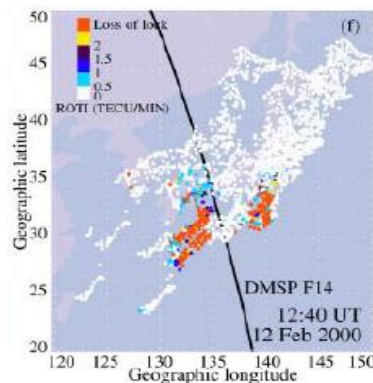




# Background (2/2)

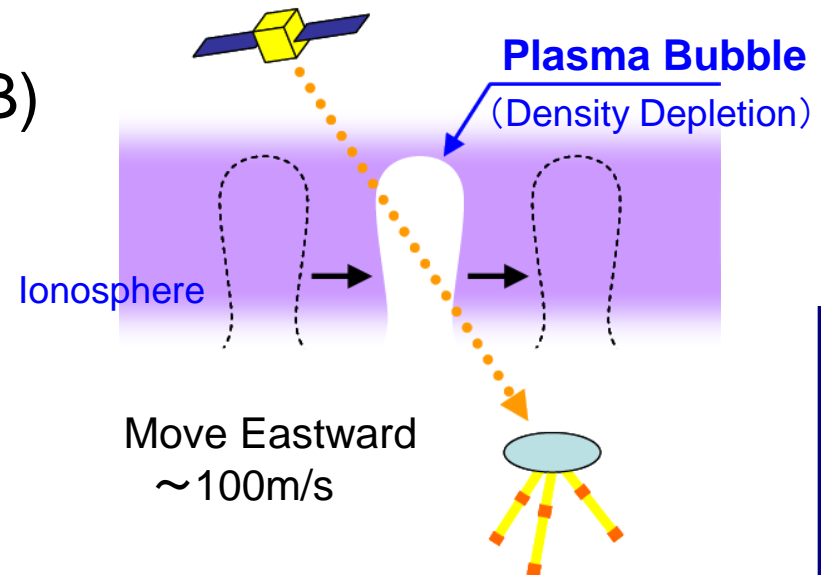
## Ionospheric Anomaly

- Storm Enhanced Density (SED) **Rare**
  - Mid~High Latitude Region
  - Spatial Gradient:  $>400\text{mm/km}$
- Equatorial Plasma Bubble (EPB) **Frequent**
  - Low~Mid Latitude Region
  - Scintillation



EPB and signal loss-of lock observed over Japan

12 Feb. 2000. Red color shows the signal loss-of lock. [Ma and Maruyama, GRL, 2006]



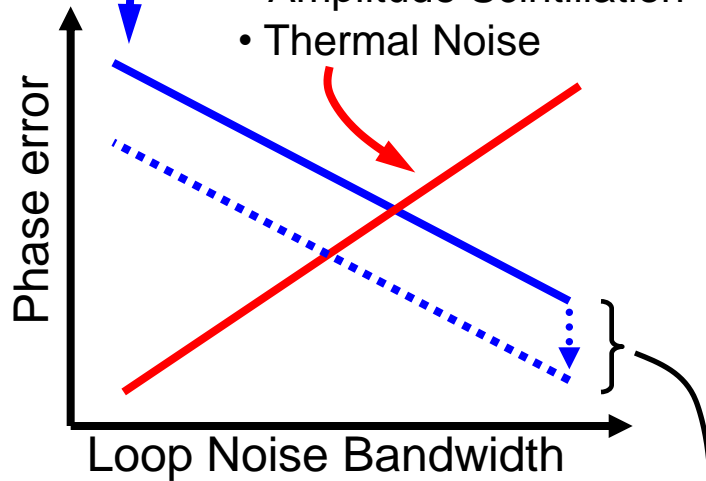


# Doppler aiding by INS

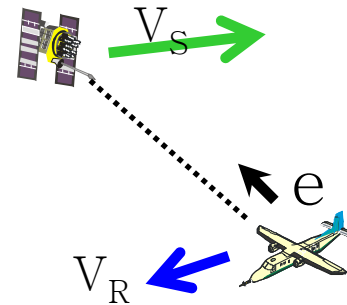
## Phase Error Sources

- Clock Dynamics
- Phase Scintillation
- Aircraft Dynamics  
**Removed by Doppler-Aiding**

- Amplitude Scintillation
- Thermal Noise

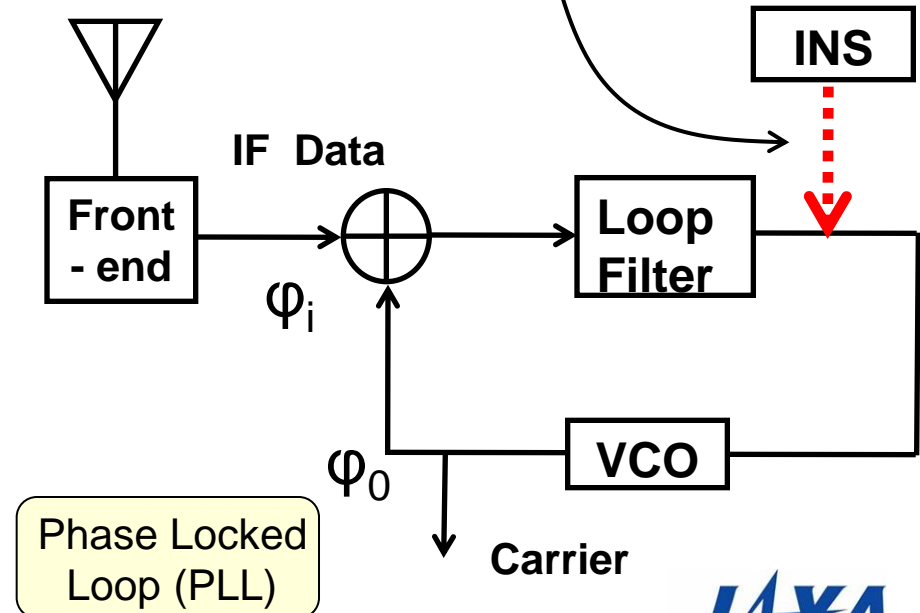


**Margin for Scintillation**



$$f_D = \frac{e \cdot (v_S - v_R)}{\lambda}$$

Doppler Frequency due to Satellite and Aircraft Dynamics



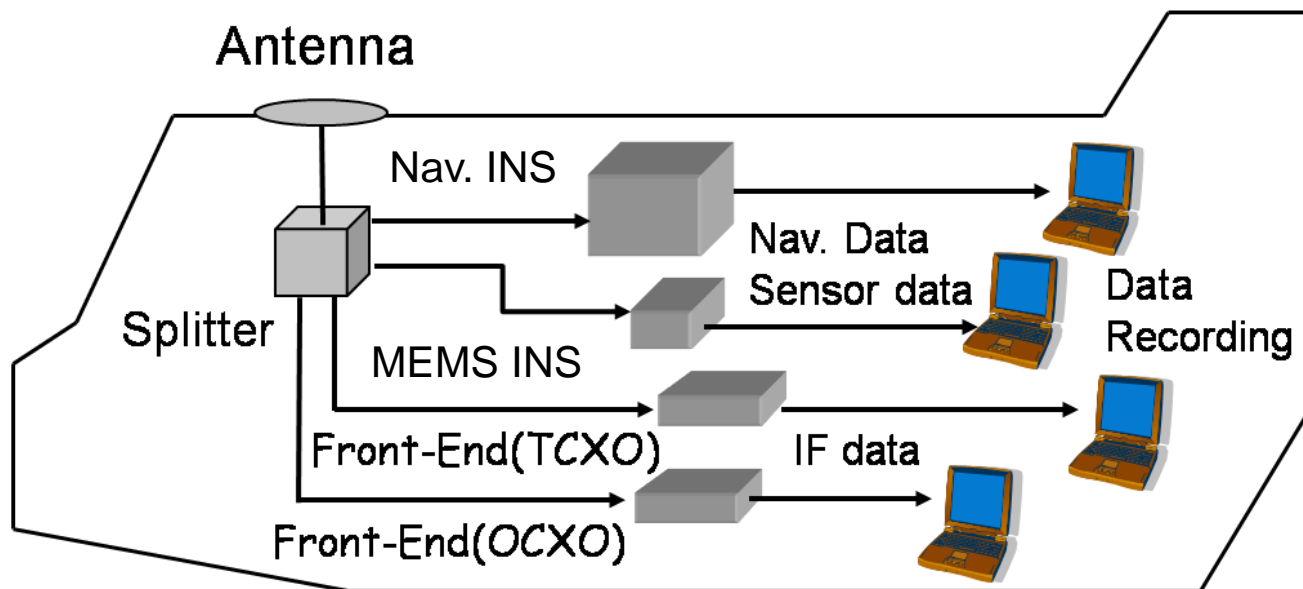
Phase Locked Loop (PLL)





# Flight test to verify fundamental function of INS-Aiding

## equipments



Nav-grade GPS/INS



MEMS GPS/INS



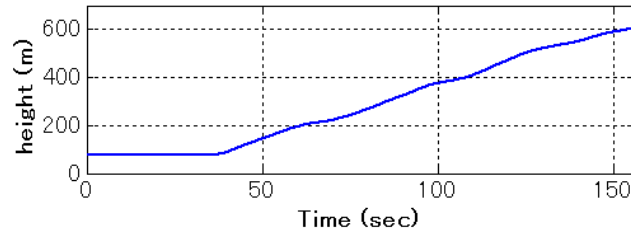
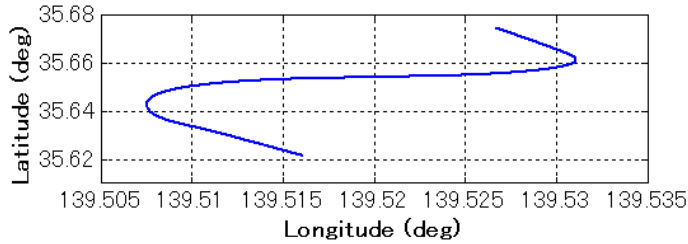
GPS Front-End (Left: TCXO, Right: OCXO)

Inter mediate Freq. data recorded  
IF frequency : 4,130,400 Hz  
sampling rate : 16,367,600 Hz

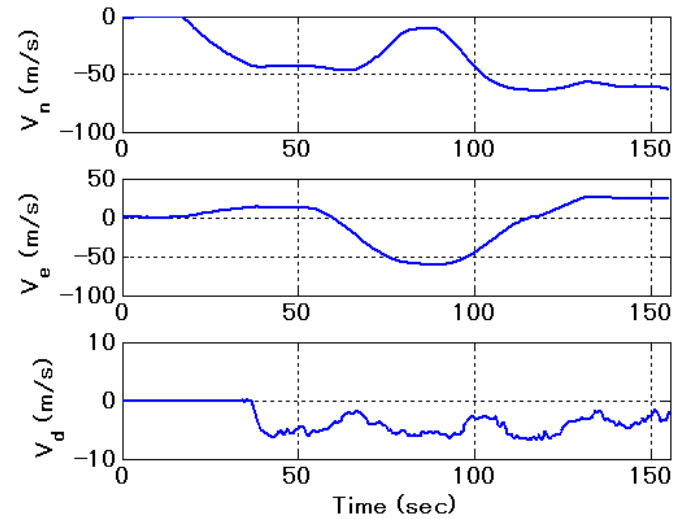


# Flight Profile – Take/Off -

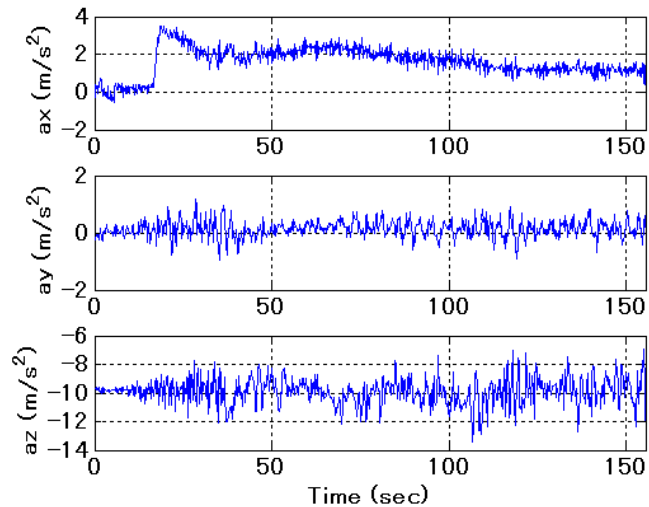
Velocity (NED)



Trajectory



Acceleration (body)



Beechcraft Model 65 QueenAir



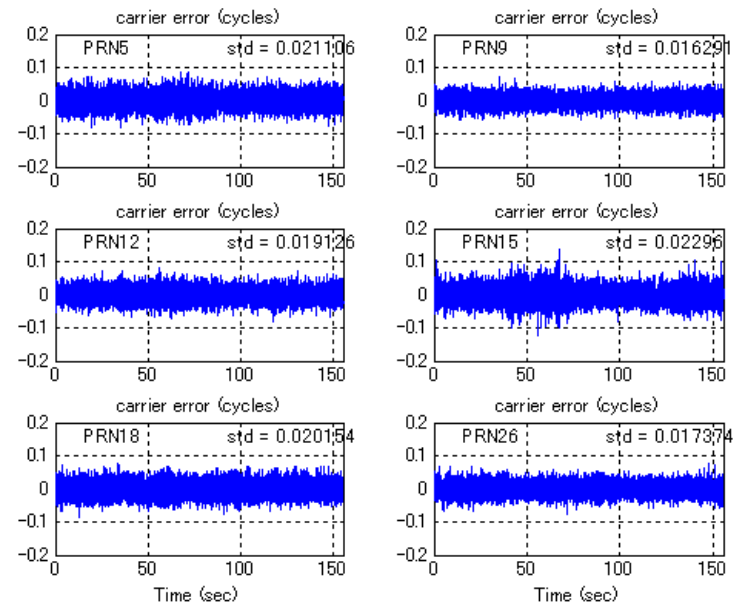
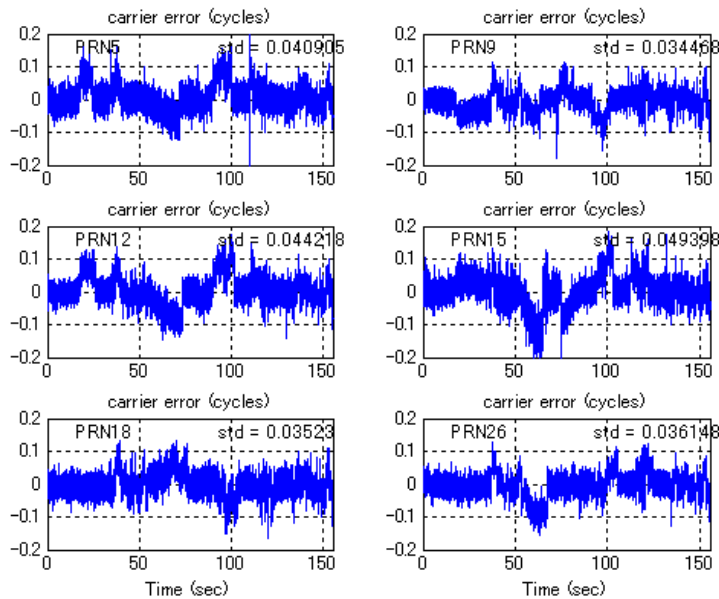


# Effect of Doppler Aiding

Carrier phase error for each satellite  
(  $B_L=3\text{Hz}$ , TCXO, MEMS-INS )

— Without Aiding —

— With Aiding —



$$\sigma_{\phi} = 7.2 \text{ mm}$$

$$\sigma_{\phi} = 3.8 \text{ mm}$$

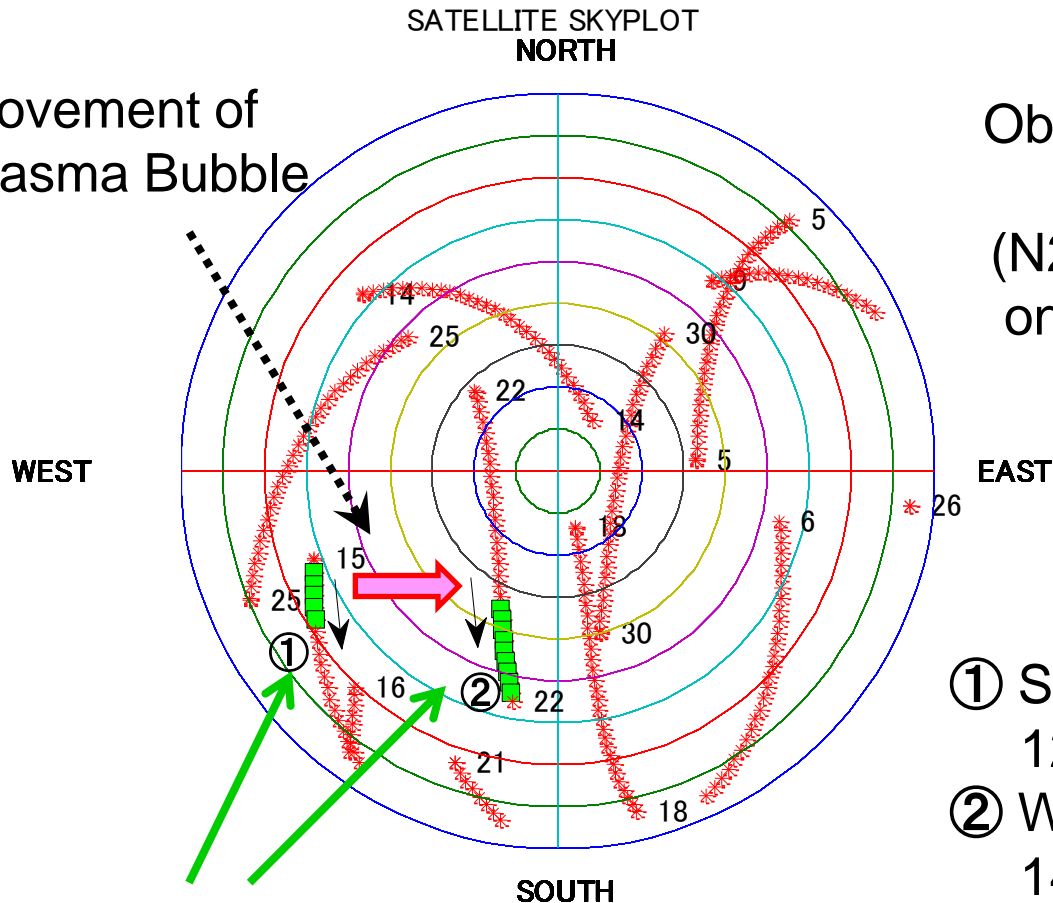
Effect of Aiding is demonstrated by using real data  
(Without Scintillation)





# Analyses of Scintillation Associated with Plasma Bubble

Movement of  
Plasma Bubble



Observation data of GSV4004  
@Naha, Japan  
(N26° 13' 43, E127° 40' 44),  
on April 14, 2004 (by ENRI)

Local Time: 9:40pm~0:05am

- ① Strong Scintillation (PRN15)  
12:40-13:10
- ② Weak Scintillation (PRN22)  
14:20-15:05 (GPS Time)

(Local Time = UT + 9 hours)

**Scintillation associated  
with Plasma Bubble**

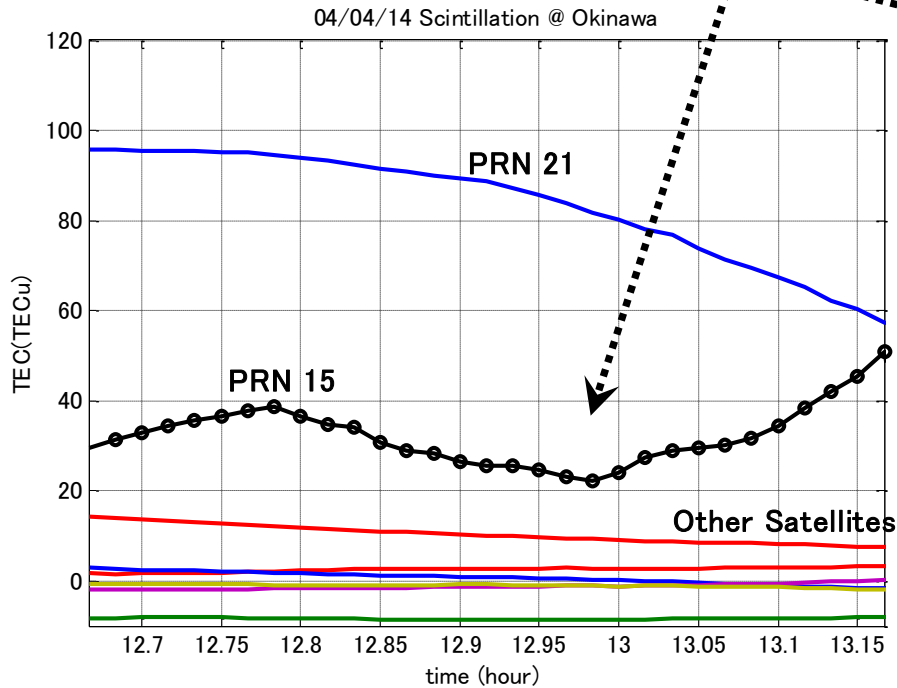




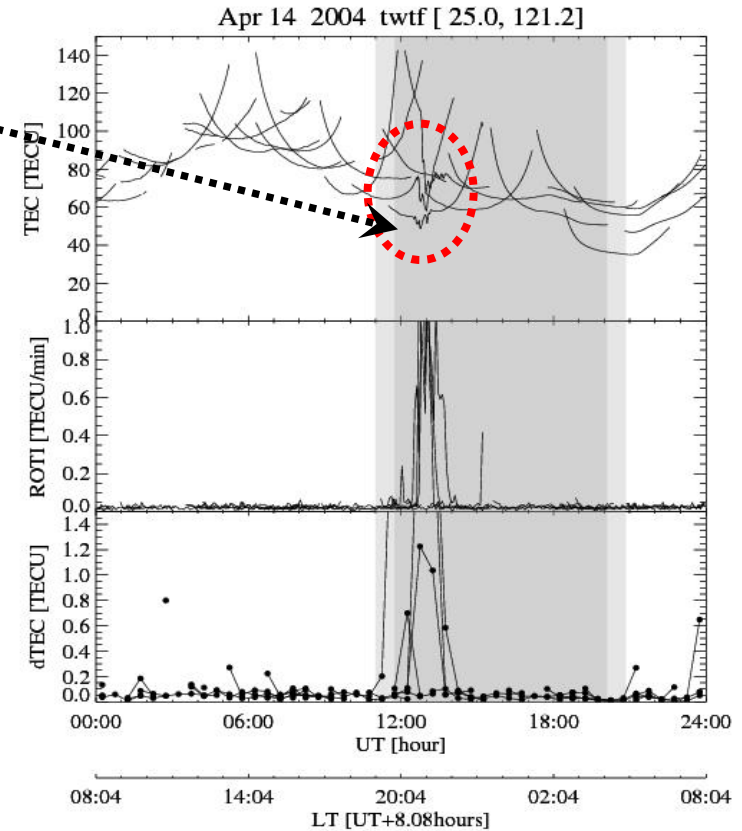


# TEC Variation during strong scintillation ①

## TEC Depletion due to Plasma Bubble



Variation of TEC @ Naha  
(bias not calibrated)



TEC variation @ Taiwan  
(<http://wdc.nict.go.jp/IONO2/TEC-ROTI/>)

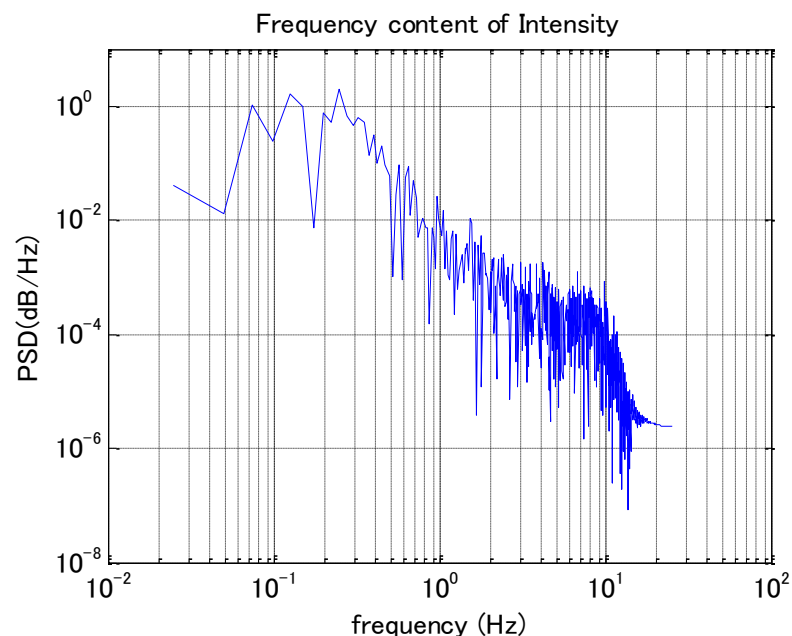
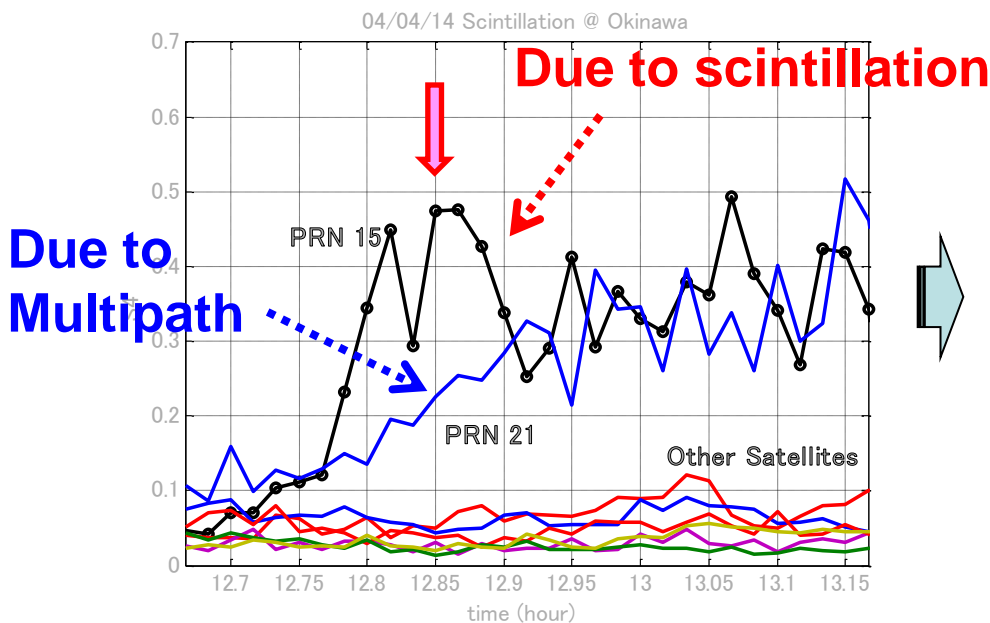




# Amplitude Scintillation Parameter and PSD of Intensity extracted from real data during Strong Scintillation ①

## S4 Variation

## Intensity spectral density (12:51)



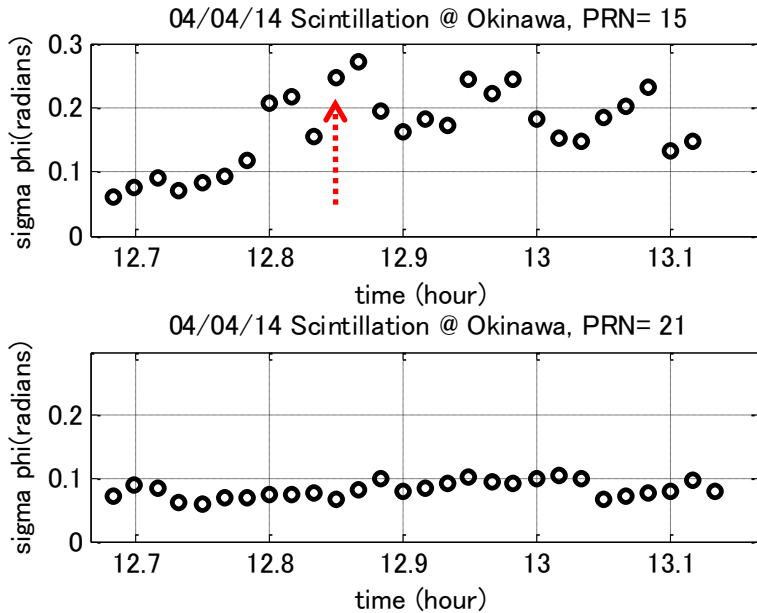
$$S4 = \sqrt{\frac{\langle I^2 \rangle - \langle I \rangle^2}{\langle I \rangle^2}}$$

Scintillation Parameters and PSD are used to simulate scintillation data

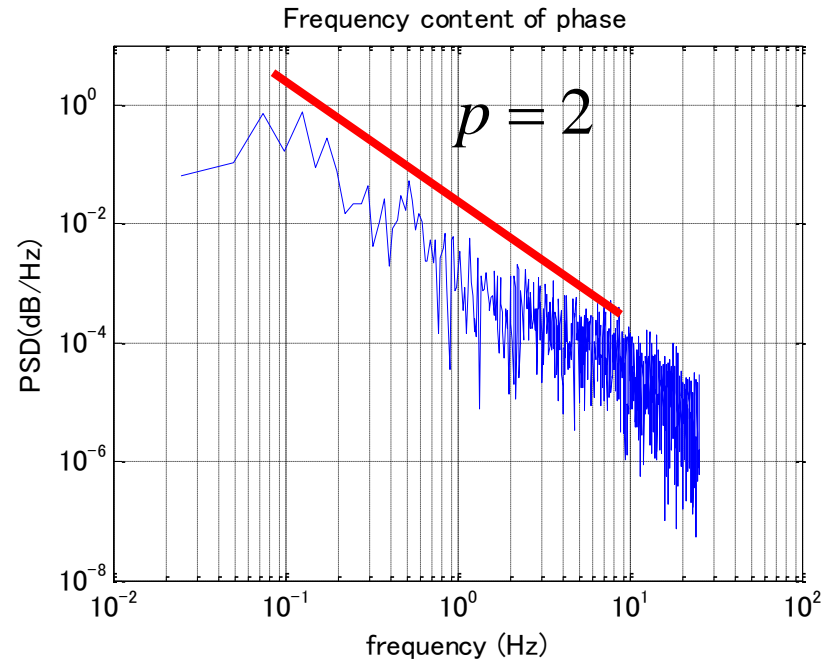


# Phase Scintillation Parameter and PSD of Phase extracted from real data during Strong Scintillation ①

## Sigma of Phase error



## Phase spectral density (12:51)

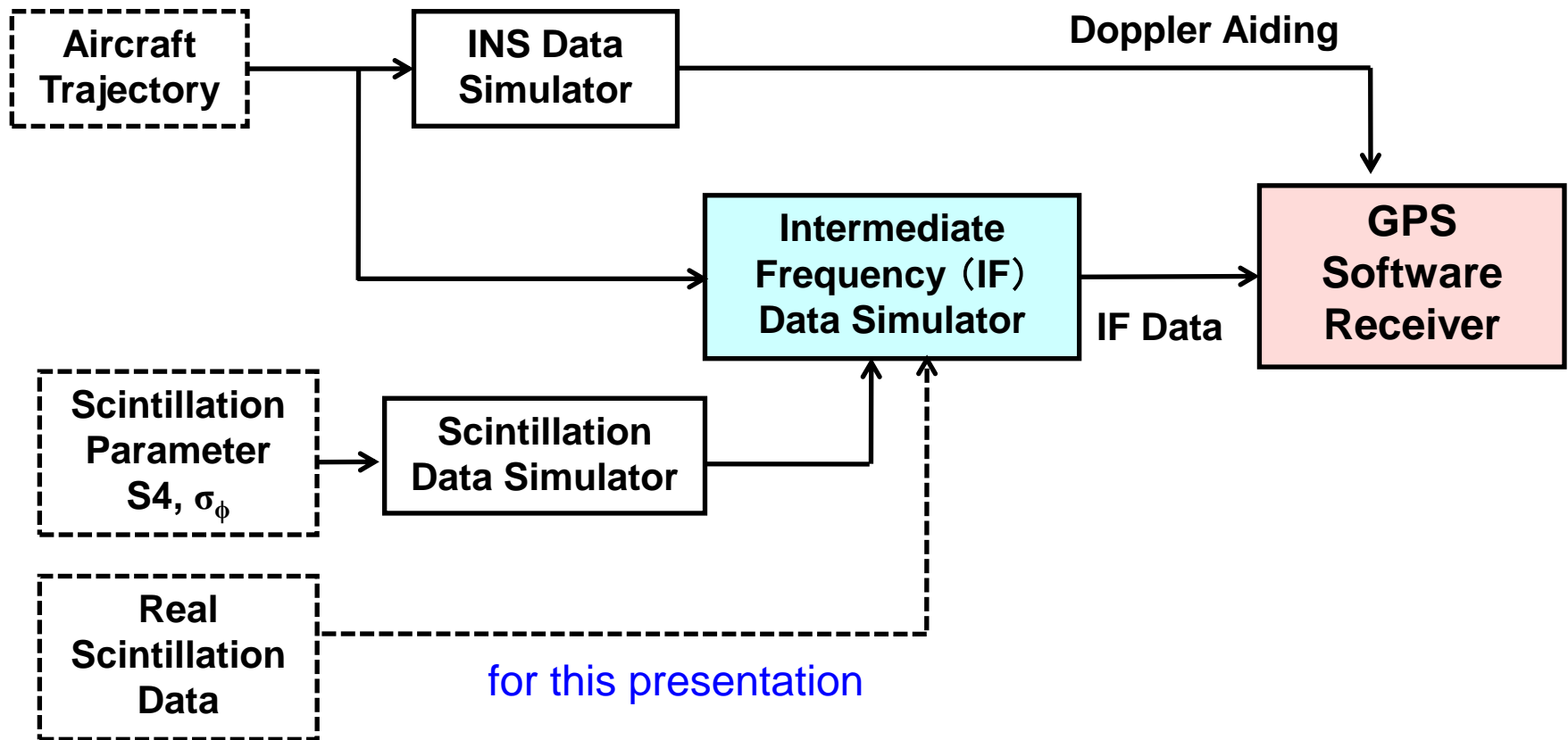


$\sigma_\phi$  for PRN15 (top)  
and PRN21 (bottom)

$$P_{\delta\phi}(f) = T \cdot f^{-p}$$

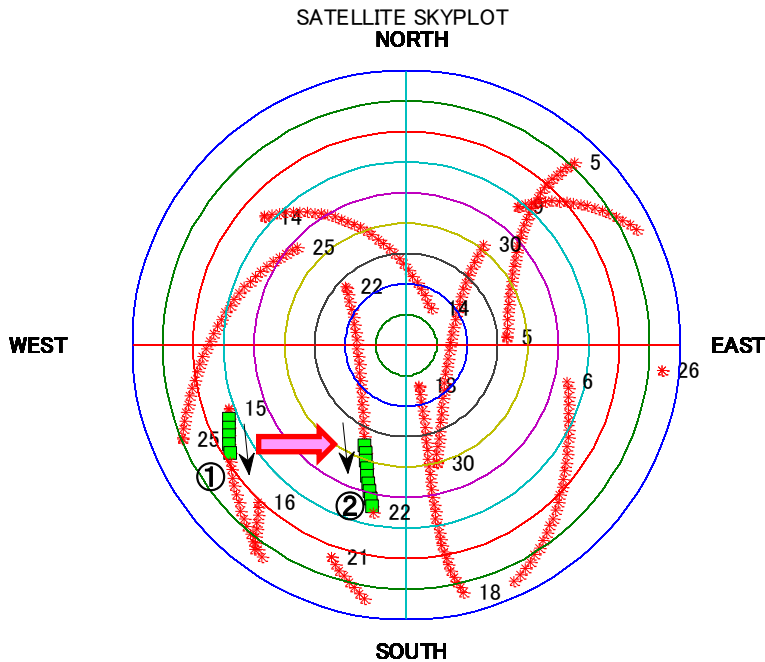


# Simulation of GPS/INS Signal Under scintillation





# Data of Weak Scintillation ②

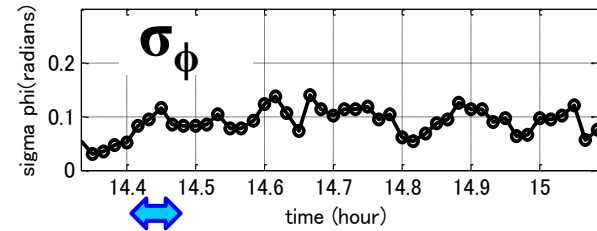
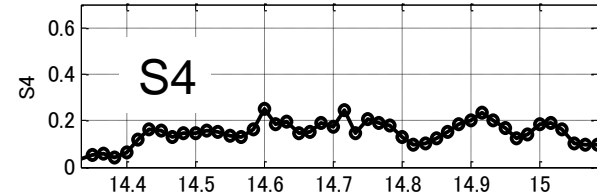
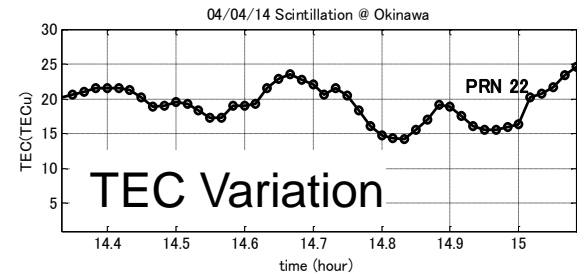


① Strong Scintillation (PRN15)

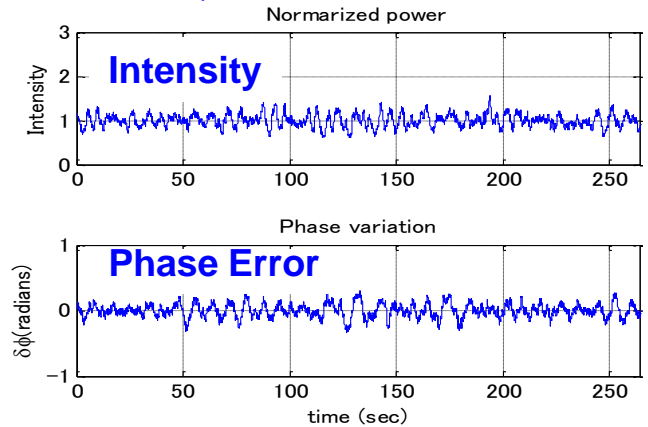
➡ **Cycle Slips for ground receiver**

② Weak Scintillation (PRN22)

Used for Simulation in this presentation



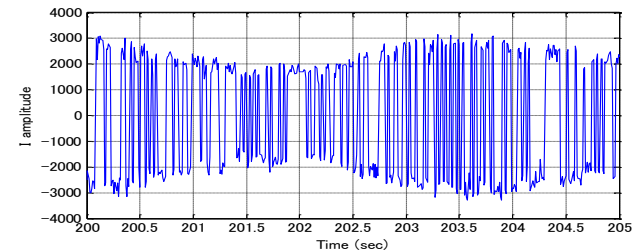
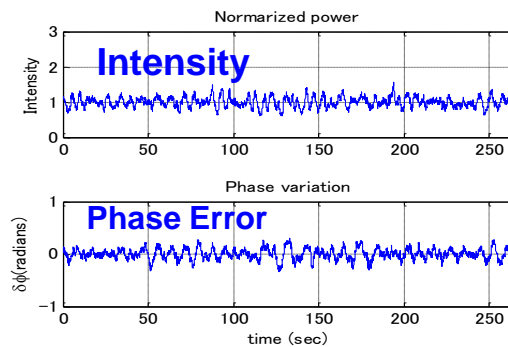
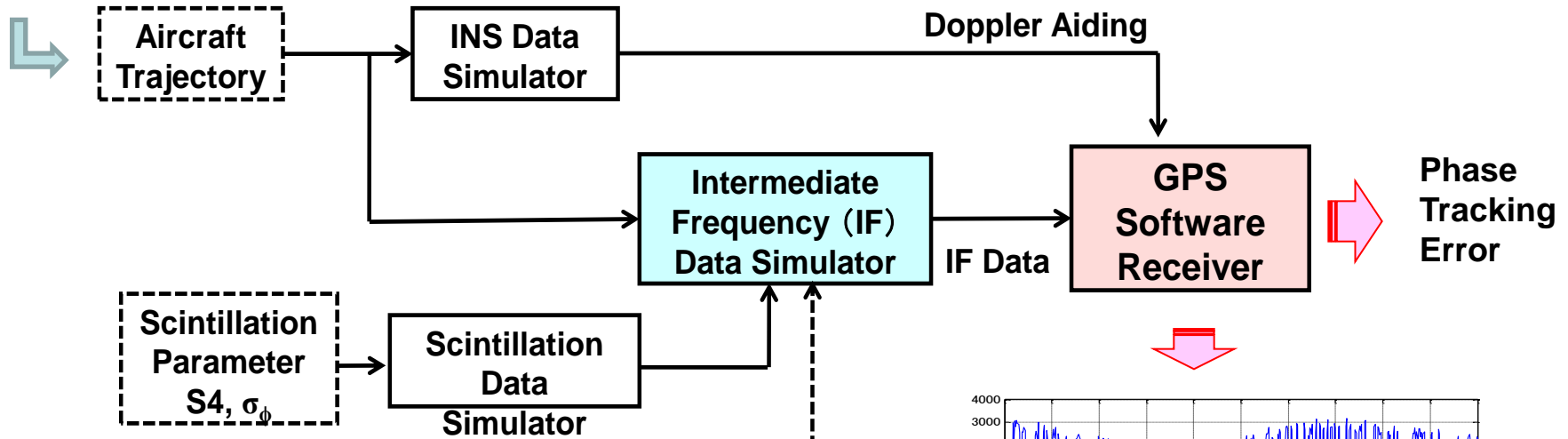
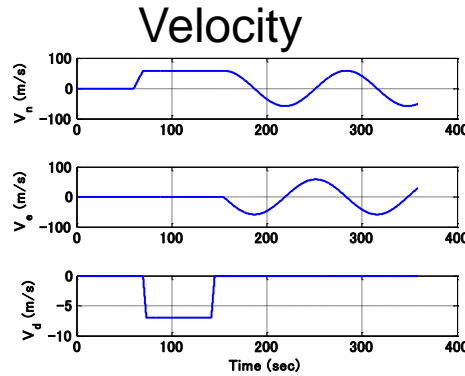
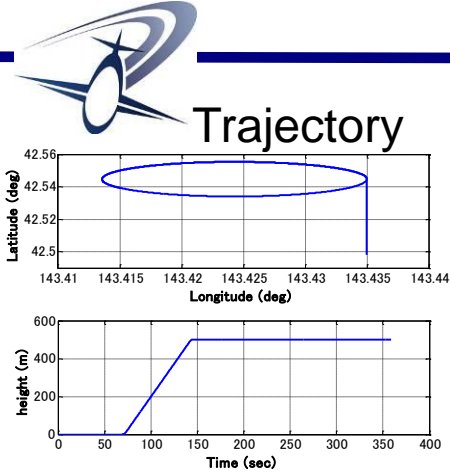
Real data (from 14h24m to 14h28m24s)



Embedded in  
Simulated IF data



# Doppler Aiding Performance Under Scintillation



I-channel Amplitude Variation due to scintillation (time from 200 to 205 seconds)





# Effect of Doppler Aiding Under Scintillation

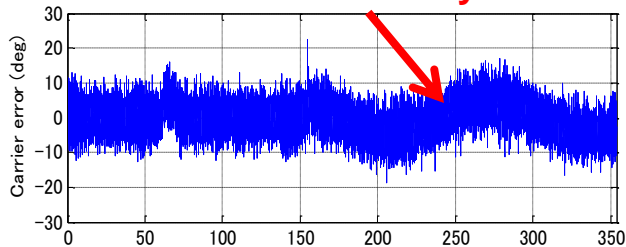
Carrier Tracking Error (deg)  
For two satellites

Without Aiding

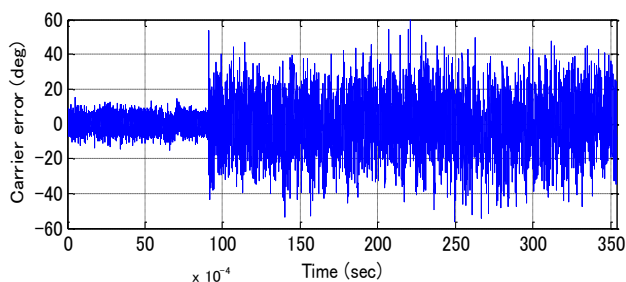
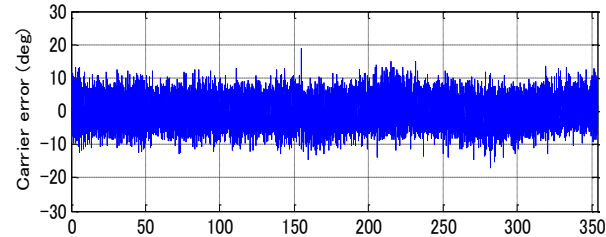


With Aiding

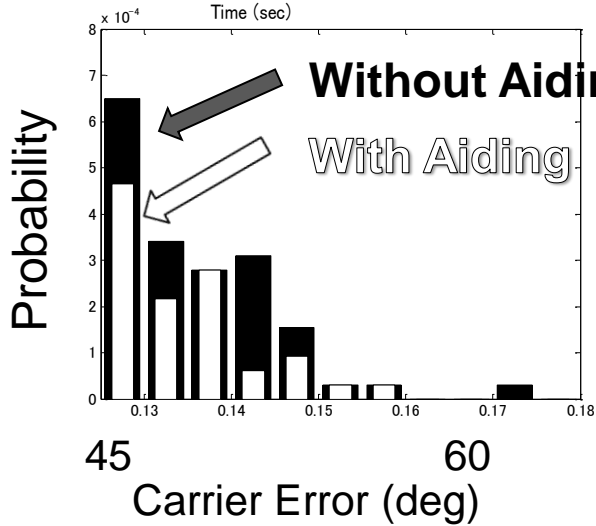
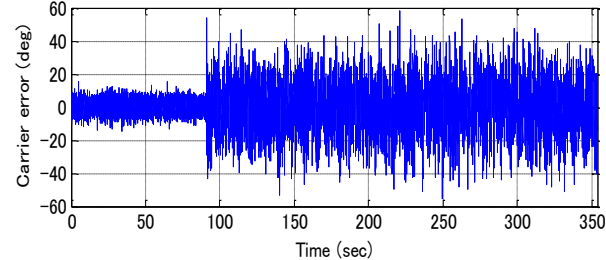
Effect of Aircraft Dynamics



Without Scintillation



With Scintillation



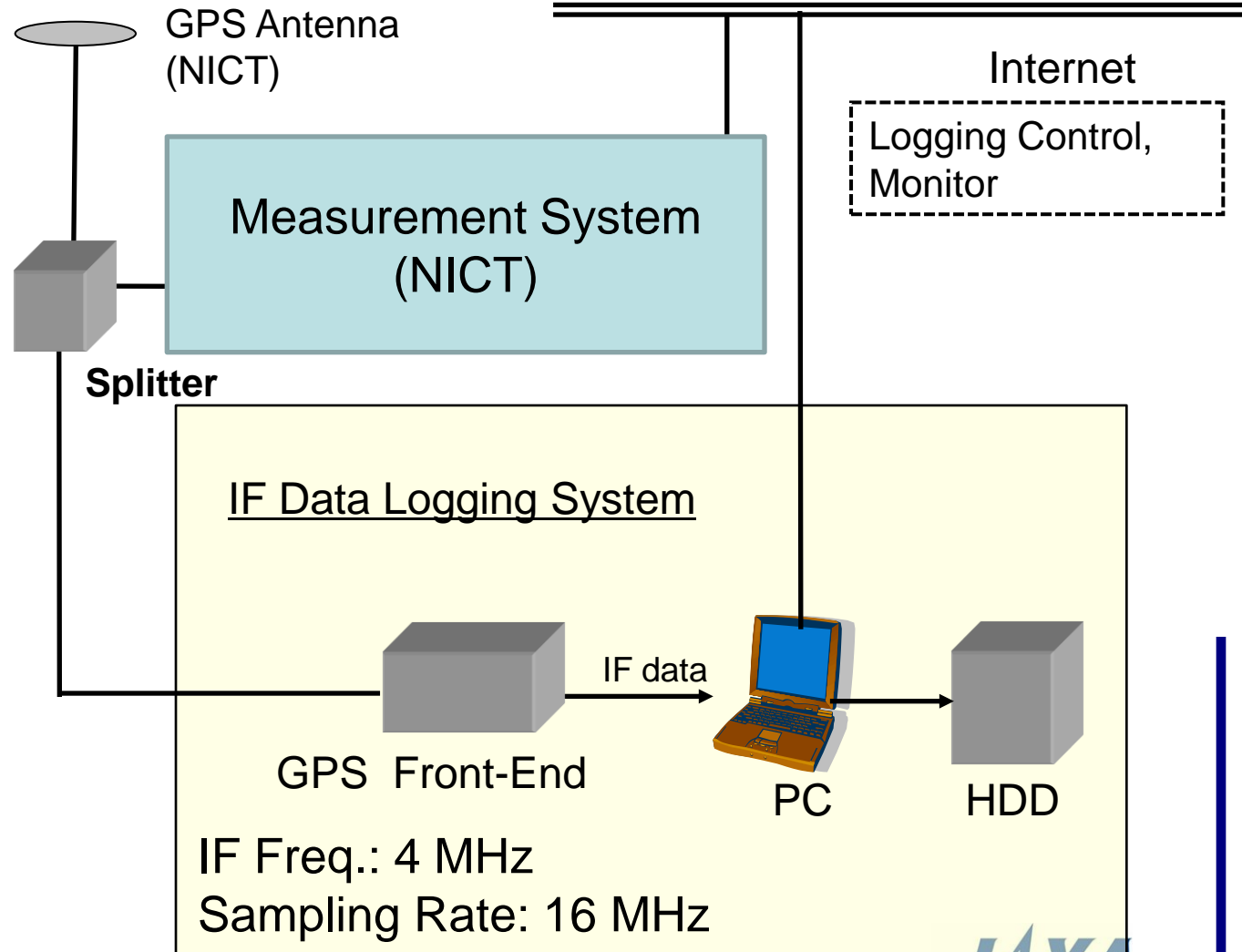
Rate of Cycle Slip  
(Carrier Error > 45 degrees)  
30 % Reduction





# GPS-IF data Logging System

@ King Mongkut's Institute of Technology (KMUTL), Bangkok







# Summary

- Real data of scintillation associated with plasma bubble was analyzed and extracted intensity/phase variation were embedded in the simulated GPS IF data
- The improvement of carrier tracking by Doppler aiding was demonstrated and an example showed that the rate of cycle slip was reduced by 30 %

## Future work

- Collect the real scintillation data (IF) and evaluate INS-Aiding performance under scintillation
- Verify the improvement of GBAS availability by INS-Aiding under scintillation associated with plasma bubble